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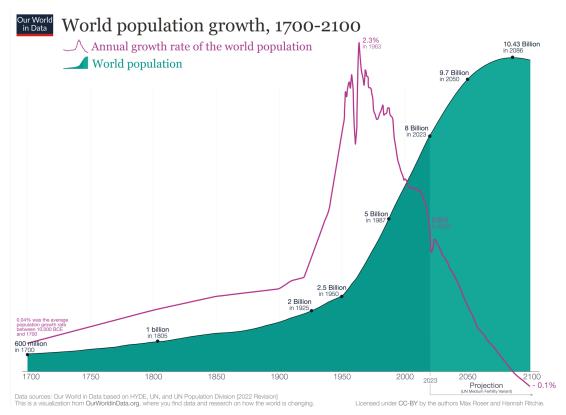
Each of us burns and blazes as best we can.
This unites us and brings us together!

AMH

## Synthesis

## Part 1. Nuclear Reactions (3 points)

According to publicly available data, the 20 th century marked the beginning of rapid population growth on our planet.



- 1. (0 points) According on the graph, determine the year when the peak population growth rate occurred, i.e., the percentage of population growth for the year was maximum, and what this rate was in percent.
- 2.  $(0.5 \ points)$  Assuming that since 2023, the population growth rate will be equal to the peak growth rate in the 20th century, determine how many years later one person will stand on each square meter of land. Assume that the Earth's radius is 6400 km and the land area is 1/3.

Due to the rapid growth of the world's population, energy consumption is also growing rapidly. Today, humanity consumes approximately  $Q = 10^{21}$  J per year. Renewable energy sources

(wind, hydro, solar, etc.) can provide up to 3Q per year, but unfortunately, they do not solve all energy problems. The energy obtained with their help is quite expensive and requires additional conditions (wind availability, a large number of sunny days per year, etc.). The power generated by these sources varies greatly over time (for example, solar panels do not generate energy at night), which requires the creation of huge and expensive energy storage facilities.

Historically, humanity has learned to actively use natural resources: oil, coal, gas, etc. Unfortunately, their reserves are limited and unevenly distributed across the planet. For example, oil reserves are about 15Q, coal reserves are about 15Q. In addition, the burning of hydrocarbons leads to the emission of greenhouse gases and affects the climate.

In addition, chemical energy sources have low energy efficiency.

3. (0.5 points) Estimate **the energy efficiency** of burning chemical fuel, i.e., the amount of energy (in eV) per nucleon released during the combustion of one kilogram of coal <sup>12</sup><sub>6</sub>C. Assume that its specific heat of combustion is 31 MJ/kg.

For these reasons, humanity is searching for alternative energy sources. In the course of research in nuclear physics, it was found that the nuclei of some elements can be transformed into the nuclei of others. For example:

$${}^{235}_{92}\mathrm{U} + {}^{1}_{0}n \longrightarrow {}^{144}_{56}\mathrm{Ba} + {}^{89}_{36}\mathrm{Kr} + 3 \, {}^{1}_{0}n,$$
$${}^{235}_{92}\mathrm{U} + {}^{1}_{0}n \longrightarrow {}^{140}_{54}\mathrm{Xe} + {}^{94}_{38}\mathrm{Sr} + 2 \, {}^{1}_{0}n.$$

- 4. (0.5 points) Using the concept of mass defect, estimate the energy efficiency of each reaction.
- 5. (0 points) By how many orders of magnitude is the energy efficiency of nuclear fuel greater than the energy efficiency of chemical fuel?

Nuclear fission reactions often produce unstable isotopes, the decay of which results in a chain of nuclear transformations.

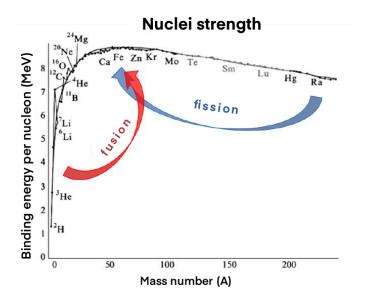
6. (1.5 points) Consider the possible decay chains of the nucleus  $^{235}_{92}$ U, at the end of which the  $^{207}_{82}$ Pb nucleus is formed. Assume that only three types of reactions are possible: alpha decay, beta-minus decay, and proton emission. Assuming that their probabilities are related as 20:10:1, respectively, determine the most likely set of decay products.

**Note.** In reality, proton emission is still an order of magnitude less likely and occurs with artificially created isotopes of chemical elements.

From all of the above, it follows that nuclear energy solves humanity's problems with energy supply. However, the operation of nuclear power plants leads to the accumulation of radioactive waste and the possibility of technological disasters, which forces us to continue the search for alternative energy sources

## Part 2. Nuclear Fusion (4 points)

It has been established that energy can be released not only during the fission of heavy nuclei but also during the fusion of light elements from the beginning of the periodic table. A visual demonstration of this fact is shown in the figure, which depicts the dependence of the binding energy of nuclei on the atomic number. It can be seen that elements to the left of Fe tend to fuse, while those to the right tend to fission.



From a practical point of view, the following fusion reactions are of most interest:

$$d+d \longrightarrow t+p+4.03 \text{ MeV},$$
  
 $d+d \longrightarrow {}_2^3\text{He}+n+3.27 \text{ MeV},$   
 $d+t \longrightarrow {}_2^4\text{He}+n+17.6 \text{ MeV},$   
 $d+{}_2^3\text{He} \longrightarrow {}_2^4\text{He}+p+18.3 \text{ MeV},$ 

where d and t are the nuclei of deuterium and tritium, respectively. It is important to note that the first and second reactions are equally probable.

1. (0 points) Find the energy efficiency of the thermonuclear fusion reactions.

Unlike fossil fuels and nuclear fuel, deuterium is widespread in nature and is found in water. There is one deuterium atom for every 6500 hydrogen atoms.

2. (0.5 points) Estimate the minimum amount of gasoline that needs to be burned to obtain energy equal to that released in the fusion reaction of deuterium extracted from one glass of water (0.33 liters). The specific heat of combustion of gasoline is 44 MJ/kg.

Consider one of the possible fusion reactions:

$$^{7}\mathrm{Li} + p \longrightarrow ^{7}\mathrm{Be} + n.$$

In this reaction, the lithium nucleus is stationary and is bombarded by protons. Such a nuclear reaction has a threshold  $E_{\rm t}=1.88~{\rm MeV}$ , i.e., it can only proceed when the kinetic energy of the proton is equal to or exceeds this value. Assume that the masses of lithium and beryllium are equal and 7 times greater than the mass of the proton and neutron. The masses of the proton and neutron are considered to be equal to 1 Da = 940 MeV/c<sup>2</sup>, where c is the speed of light. Express momentum in MeV/c.

- 3. (0.5 points) Counting the collisions of proton and lithium, find the neutron momentum if the proton energy is  $2E_{\rm t}$ .
- 4. (0.5 points) At what value of the energy of the incoming proton is the process possible when the neutron is stationary?

- 5. (1 point) The collision of the proton and lithium is off-center. At what value of the incoming proton energy will the maximum angle at which the neutron can start moving relative to the proton velocity be equal to  $\pi/6$ ?
- 6. (1 point) The proton energy is the same as in the previous point. It is known that neutrons with two energy values are detected in the direction  $\varphi$  at the proton velocity. One type of neutron has energy  $E_1$ . What is the second energy value,  $E_2$ ?
- 7. (0.5 points) Estimate the Coulomb interaction energy of the proton and the lithium nucleus when they approach each other closely. The classical radius of an atomic nucleus is  $1.4 \cdot 10^{-15} \sqrt[3]{A}$  m, where A is the mass number. Assume that proton is a point particle.

For nuclear fusion reactions to occur, the Coulomb barrier of repulsion between interacting particles must be overcome. Therefore, for the implementation of controlled thermonuclear fusion, it is preferable to use hydrogen isotopes, which have the smallest charge among all other nuclei. However, even for them, thermonuclear fusion reactions can only proceed at very high temperatures, on the order of tens of keV (1 eV = 11604 eV). At such temperatures, any substance transitions into a plasma state.

When creating a fusion reactor, it is necessary to solve two main problems. The first is to confine the plasma with the required parameters for a sufficiently long time, and the second is to prevent the flow of heat and particles from damaging the reactor walls. Both of these issues are addressed through the use of magnetic fields and are analyzed in the 11th-grade problem.

In the 9th-grade problem, we will get acquainted with the concept of plasma using the example of a self-sustained gas discharge. The process of maintaining the discharge involves a positive feedback mechanism, which in one form or another is found in any generator, including a fusion power plant (yes, it is also a generator).

## Part 3. Self-Sustained Discharge (3 points)

Let's qualitatively consider the process of the emergence of a self-sustained gas discharge.

The space between two flat conducting electrodes (cathode and anode), located at a distance d from each other, is filled with gas, and the electrodes themselves are connected to a DC voltage source.

The process of gas discharge formation consists of two parts. The first is the formation by electrons in the process of ionization of the current of electrons and ions in the medium filling the space between the electrodes. The second part is the knocking out of new secondary electrons by ions from the cathode.

Let's consider each of these processes in more detail.

Suppose that, for some reason, an electron is formed between the electrodes. Under the action of an electric field, it begins to accelerate and move from the cathode to the anode, colliding with gas molecules and ionizing them in the process. The new formed electrons and ions will also move towards the anode and cathode, respectively. At the same time, electrons will create more and more new electron-ion pairs, while ions will not (since their speed, which is one of the determining parameters in this process, will be significantly lower than the speed of electrons). For this reason, if nothing happens when ions hit the cathode, then after a while the process of current flow in the gas will stop, because all electrons will reach the anode, ions will reach the cathode, and new charges will not be formed.

However, when an ion hits the cathode, with a certain probability, electrons are knocked out, which again starts the process of electron-ion pair formation in the gas.

In this section, you are invited to explore this process.

Let's call the volume ionization coefficient  $\alpha$  the number of electron-ion pairs formed per unit length of the electron path, and the coefficient of secondary ion-electron emission  $\gamma$  is the average number of electrons knocked out of the cathode by one ion. By external ionization, we mean some process that creates primary electrons. These can be a variety of processes: ultraviolet or  $\gamma$  radiation passing through the gas, an additional conductor creating a small current of electrons, and so on. In our review, we will assume that this process is localized in the cathode region.

- 1. (0.5 points) It is known that the electron current in the cathode region is  $I_{ek}$ , which includes the external ionizer current and the current of secondary electrons knocked out of the cathode by ions. The volume ionization coefficient  $\alpha$  is known and constant throughout the volume between the electrodes. Find the electron current in the anode region.
- 2. (0.5 points) Determine the ion current in the cathode region  $I_{ik}$ .
- 3. (1 point) Express the cathode and anode electron currents  $I_{ek}$  and  $I_{ea}$  in terms of the ionization current  $I_i$ .

Breakdown is a situation where the electron current  $I_{ea}$  grows infinitely with an arbitrarily small ionization current. If, after the breakdown occurs, the external ionizer is removed and the current does not stop, then the discharge is called self-sustained: ionization is maintained by processes in the discharge itself.

4. (1 point) Determine under what circumstances on  $\alpha$ ,  $\gamma$ , and d breakdown will occur and the discharge will become self-sustained.

**Note.** You might find useful the following fact:

$$(e^{\alpha x})' = \alpha e^{\alpha x}.$$

First hint  $-29.05.2024\ 20:00\ (Moscow\ time)$ Second hint  $-31.05.2024\ 12:00\ (Moscow\ time)$ 

Final of the fifth round -02.06.2024 18:00 (Moscow time)